

NodeLab: A MATLAB package for meshfree node-generation and adaptive refinement

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Summary

Many real-world applications (like weather forecasting, tsunami modeling, geophysical imaging, and computational mechanics) require generating large number of nodes in arbitrary domains as a vital step for meshfree numerical modeling.

NodeLab is a simple MATLAB repository for node generation and adaptive refinement for testing, and implementing various meshfree methods for solving PDEs in arbitrary 2D domains. The core algorithm behind this package is the 'node-placing' approach (Fornberg & Flyer, 2015) because of its simplicity, computational speed, and the quality of the distribution. The 'node-placing' method has been used for creating an initial node-distribution in the boundingbox of the desired domain. A crucial decision in this context is how to represent the geometry of the domain. We compute the signed-distance field (SDF) for the domain geometry based on a priori information about the domain, which is often used in mesh-generation for finite element methods (Persson & Strang, 2004). This a priori information could be the geometry created using simple shapes, given as a function D(x,y) = 0, or some discrete set of seed nodes—later providing the flexibility to create the domain by manually digitizing the geometry. Refinement of the boundary nodes is done by formulating the problem in terms of differential equations that describe the path along the curve and interpolating through an ODE solver. The node distribution in NodeLab can be refined non-uniformly by adapting the information provided through 'control-points', which are an input from the user. 'control-points' provide spatial locations where the user needs relatively finer nodes.

Future developments in this package may include its extension to 3D and surfaces, an optional graphical user interface, and improvements to adaptivity by using machine learning algorithms to decide the 'control-points'. NodeLab is intended to be an open-source and collaborative project, where developers and users could contribute to make (and keep) it state-of-the-art by incorporating the improvements as the research in this field grows with time.

References

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Software

- Review 🗗
- Repository C
- Archive C

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